

Derived Quantities

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- What are "derived quantities?"
- A quick tour of some of the routines provided for the computation of derived quantities
 - Vector/Matrix Routines
 - Geometry Routines
 - Coordinate System Routines
 - Lighting angles, intercepts and season
 - Geometry-finder Routines
- Examples of use:
 - Computing Illumination Angles
 - Computing Ring Plane Intercepts
 - Computing Occultation Events



What are Derived Quantities?

- Derived quantities are produced using data from kernels
 - These are the primary reason that SPICE exists!
- Examples are:
 - Angles, Angular Rates
 - Distances, Speeds
 - Directions
 - Lighting conditions
 - Cartographic parameters (LAT/LON)
 - Time windows of events
- The SPICE Toolkit contains many routines that assist with the computations of derived quantities.
 - Some are fairly low level, some are quite high level.
 - More are being added as time permits.





A Quick Tour

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Vector/Matrix Routines

- Vector and vector derivative arithmetic
- Matrix arithmetic
- Geometric "Objects"
 - Planes
 - Ellipses
 - Ellipsoids
 - Rays

Coordinate Systems

- Spherical: latitude/longitude, co-latitude/longitude, right ascension/declination; Geodetic, Cylindrical, Rectangular, Planetographic
- Others

The lists on the following pages are just a subset of what's available in the Toolkit.





- Function
 - _ <v,w>
 - **v** x **w**
 - v/|v|
 - $-\mathbf{v} \times \mathbf{w} / |\mathbf{v} \times \mathbf{w}|$
 - v+w
 - v-w
 - av [+ bw [+ cu]]
 - angle between v and w
 - **|v|**

- Routine
 - VDOT, DVDOT
 - VCROSS, DVCRSS
 - VHAT, DVHAT
 - UCROSS, DUCRSS
 - VADD, VADDG
 - VSUB, VSUBG
 - VSCL, [VLCOM, [VLCOM3]]
 - VSEP
 - VNORM



- VPROJ, VPERP

- TWOVEC, FRAME



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Selected Matrix-Vector Linear Algebra Routines

Function	<u>Routine</u>
– M x v	- MXV
— M x M	– MXM
$- \mathbf{M}^{t} \mathbf{X} \mathbf{V}$	– MTXV
$- \mathbf{M}^{t} \times \mathbf{M}$	– MTXM
– M x M ^t	– MXMT
$- \mathbf{v}^{t} \mathbf{X} \mathbf{M} \mathbf{X} \mathbf{v}$	- VTMV
— M ^t	- XPOSE
− M ⁻¹	- INVERSE, INVSTM

M = Matrix
V = Vector
X = Multiplication
T = Transpose



Matrix Conversions







Routine

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Function

Ellipsoids • nearest point - NEARPT, SUBPNT, DNEARP - surface ray intercept - SURFPT, SINCPT - surface normal - SURFNM – limb - EDLIMB - slice with a plane - INELPL - altitude of ray w.r.t. to ellipsoid - NPEDLN Planes • intersect ray and plane - INRYPL Ellipses • project onto a plane - PJELPL - find semi-axes of an ellipse - SAELGV



Coordinate Transformation	Routine
 Latitudinal to/from	- LATREC
Rectangular	RECLAT
 Planetographic to/from Rectangular 	 PGRREC RECPGR
 R.A. Dec to/from	- RADREC
Rectangular	RECRAD
 Geodetic to/from	- GEOREC
Rectangular	RECGEO
 Cylindrical to/from	- CYLREC
Rectangular	RECCYL
 Spherical to/from	- SPHREC
Rectangular	RECSPH



- <u>Coordinate</u>
 <u>Transformation</u>
 - Latitudinal to/from Rectangular
 - Planetographic to/from Rectangular
 - R.A. Dec to/from Rectangular
 - Geodetic to/from Rectangular
 - Cylindrical to/from Rectangular
 - Spherical to/from Rectangular

- Jacobian (Derivative) Matrix Routine
 - DRDLAT DLATDR
 - DRDPGRDPGRDR
 - DRDLAT* DLATDR*
 - DRDGEO
 DGEODR
 - DRDCYL DCYLDR
 - DRDSPHDSPHDR
 - * Jacobian matrices for the R.A and Dec to/from rectangular mappings are identical to those for the latitudinal to/ from rectangular mappings



- Example: transform velocities from rectangular to spherical coordinates using the SPICE Jacobian matrix routines. The SPICE calls that implement this computation are: CALL SPKEZR (TARG, ET, REF, CORR, OBS, STATE, LT)
 CALL DSPHDR (STATE(1), STATE(2), STATE(3), JACOBI)
 - CALL MXV (JACOBI, STATE(4), SPHVEL)
- After these calls, the vector SPHVEL contains the velocity in spherical coordinates: specifically, the derivatives

(d (r) / dt, d (colatitude) / dt, d (longitude) /dt)

- Caution: coordinate transformations often have singularities, so derivatives may not exist everywhere.
 - Exceptions are described in the headers of the SPICE Jacobian matrix routines.
 - SPICE Jacobian matrix routines signal errors if asked to perform an invalid computation.



- Illumination angles (phase, incidence, emission)
 - ILUMIN*
- Subsolar point
 - SUBSLR*
- Subobserver point
 - SUBPNT*
- Surface intercept point
 - SINCPT*
- Longitude of the sun (L_s), an indicator of season
 LSPCN

* These routines supercede the now deprecated routines ILLUM, SUBSOL, SUBPT and SRFXPT



Geometric Events Finder

- Most SPICE routines are used to determine a quantity at a specified time.
- The SPICE Geometry Finder (GF) subsystem takes the opposite approach: find times, or time spans, when a specified geometric condition or event occurs.
 - This is such a large topic that a separate tutorial ("geometry_finder") has been written for it.





• On the next several pages we present examples of using some of the "derived quantity" APIs.



 Given the direction of an instrument boresight in a bodyfixed frame, return the illumination angles (incidence, phase, emission) at the surface intercept on a tri-axial ellipsoid





Computing Illumination Angles



- CALL <u>GETFOV</u> to obtain boresight direction vector
- CALL <u>SINCPT</u> to find intersection of boresight direction vector with surface
- CALL <u>ILUMIN</u> to determine illumination angles



 Determine the intersection of the apparent line of sight vector between Earth and Cassini with Saturn's ring plane and determine the distance of this point from the center of Saturn.



Computing Ring Plane Intercepts-2

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This simplified computation ignores the difference between the light time from Saturn to the earth and the light time from the ring intercept point to the earth.

The position and orientation of Saturn can be re-computed using the light time from earth to the intercept; the intercept can be re-computed until convergence is attained. This computation is for the reception case; radiation is received at the earth at a given epoch "ET".

- CALL <u>SPKEZR</u> to get light time corrected position of spacecraft as seen from earth at time ET in J2000 reference frame SCVEC.
- CALL <u>SPKEZR</u> to get light time corrected position of center of Saturn at time ET as seen from earth in J2000 frame SATCTR.
- CALL <u>PXFORM</u> to get rotation from Saturn body-fixed coordinates to J2000 at light time corrected epoch. The third column of this matrix gives the pole direction of Saturn in the J2000 frame SATPOL.
- CALL <u>NVP2PL</u> and use SATCTR and SATPOL to construct the ring plane RPLANE.
- CALL <u>INRYPL</u> to intersect the earth-spacecraft vector SCVEC with the Saturn ring plane RPLANE to produce the intercept point X.
- CALL <u>VSUB</u> to get the position of the intercept with respect to Saturn XSAT (subtract SATCTR from X) and use <u>VNORM</u> to get the distance of XSAT from the center of Saturn.

Computing Ring Plane Intercepts-3

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An alternate approach

- Create a dynamic frame with one axis pointing from earth to the light time corrected position of the Cassini orbiter. Use the CN correction for this position vector. (This gives us a frame in which the direction vector of interest is constant.)
- Temporarily change the radii of Saturn to make the polar axis length 1 cm and the equatorial radii 1.e6 km. This can be done either by editing the PCK or by calling <u>BODVCD</u> to fetch the original radii, then calling <u>PDPOOL</u> to set the kernel pool variable containing the radii to the new values. This flat ellipsoid will be used to represent the ring plane.
- Use <u>SINCPT</u> to find the intercept of the earth-Cassini ray with the flat ellipsoid. Use the CN correction. SINCPT returns both the intercept in the IAU_SATURN frame and the earth-intercept vector. Use <u>VNORM</u> to get the distance of the intercept from Saturn's center.
- Restore the original radii of Saturn. If PDPOOL was used to update the radii in the kernel pool, use <u>PDPOOL</u> again to restore the radii fetched by BODVCD.



 Determine when the spacecraft will be occulted by an object (such as a natural satellite) as seen from an observer (such as earth).





Find Occultation Ingress/Egress



- Select a start epoch, stop epoch and step size.
 - Start and stop epochs can bracket multiple occultation events
 - Step size should be smaller than the shortest occultation duration of interest, and shorter than the minimum interval between occultation events that are to be distinguished, but large enough to solve problem with reasonable speed.
 - Insert search interval into a SPICE window.
 This is the "confinement window."
- CALL <u>GFOCLT</u> to find occultations, if any. The time intervals, within the confinement window, over which occultations occur will be returned in a SPICE window.
 - GFOCLT can treat targets as ellipsoids or points (but at least one must be an ellipsoid).
 - GFOCLT can search for different occultation or transit geometries: full, partial, annular, or "any."